# **Optimal Train Operation Adjustment under Service Disruptions**

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**Abstract.** Train service disruptions can be caused by unexpected situation in operation, which lead to large-scale train delays and passenger stranded. In this paper, the service disruption that is caused by the down train having fault in the section is described. According to the section where the fault train stops and the operating processes of trains, rescue plan is determined. Meanwhile, in order to alleviate the train delays and stranded passengers, the short-turning strategy is used for adjustment. Based on the delay caused by fault and the turning-back stations in the line, turning-back strategies can be determined and the effects of reducing stranded passenger and delay time are compared to determine the optimal turning-back strategy. On the other hand, the strategy which just adjusts headway and stopping time after line reopen is also used. Compared with two strategies simulation results, the short-turning strategy is faster to reduce passenger retention and resume normal operation.

Keywords: train schedule, train rescue, operation adjustment, short-turning

# 1. Introduction

During the daily operation of urban rail transit, disruptions occur due to an increase of the capacity demand, infrastructure malfunctioning or emergencies in operation. Some disruptions may result in trains can't passing sections. Therefore, it is necessary to organize the short-turning operation by using parking lines, crossing line or turning-back lines to maintain operation of trains [1]. In [2], the frequencies of trains are analysed by short-turning strategy, meanwhile, timetable calculation is not taken into consideration. The strategy that a short-turning without stopping at intermediate stations is studied in [3], however, stranded passengers are not able to be absorbed quickly. In [4], short-turning is applied not as a means of dealing with usual demand conditions, but as a method to manage passenger overloads after an episode of demand increase. In [5], short-turning strategy is used in operation disruption, according to the location and range of the fault sections, there are usually three adjustment strategies, they are shown in the Fig.1, Fig.2 and Fig.3.



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Fig.3: Short-turning in one side.

This paper takes a train fault in section as an example, in order to move the fault train and recover normal operation, another train is organized to rescue [6]. During rescue process for the fault train, short-turning strategy shown in Fig.1 is used to maintain operation. The regulation with short-turning strategy will be simulated, and departure and arrival time, dwell time will be obtained by means of an optimization model.

# 2. Problem Formulation

## 2.1. Model Parameters

To formulate the operation adjustment problem, the following notations in table 1 will be used before we get the mathematical model.

S <sub>t</sub> T <sub>r</sub>	Stations and trains in the line
$Ar_i^i ar_i^i$	Scheduled and actual arrival time of $i \in T_r$ train at station j
De <sup>i</sup> de <sup>i</sup>	Scheduled and actual departure time of train $i \in T_r$ at station <i>j</i>
$R_{i,j}^0 R_{i,j}$	Scheduled and actual running time of train $i \in T_r$ of section j
t <sub>min j</sub> t <sub>max j</sub>	Minimum and maximum stopping time at station $j \in S_t$
$T_{hwmin} T_{hwmax}$	Minimum and maximum headway between two trains
$a_u a_d$	Train acceleration and deceleration
R <sub>min j</sub>	Minimum running time of section <i>j</i>
$P_m$	Max passengers load of a train
$Vf_i$	Number of passengers entering station per second
$P_{i,i}$	Passengers of train $i \in T_r$ at station $j \in S_t$
$Fo_{j}^{i}$	The number of the passengers detained on the platform when the train $i$
-	departs from station j
$S_a$	The distance from the station where passengers on rescue train off to the
	position where fault train stops
$S_c$	The distance from the station where passengers on fault train off to
	specific storage
Т	Total time of the rescue
$V_r V_h$	Normal running speed and speed after fault train and rescue train coupling

Table 1: Model parameters

## 2.2. Train Delay Time Model

The following trains are unable to operate normally and will be delay because of disposing the fault, the disposing time T, i.e., the delay time is determined by  $T_c$ ,  $T_a$ ,  $T_h$ ,  $T_p$ ,  $T_f[7]$ .

$$T = T_c + T_a + T_h + T_p + 2 * T_f$$
(1)

 $T_c$ : The time from fault occurring to being confirmed;

 $T_a$ : The time from rescue train being informed to arriving at the fault spot;

 $T_h$ : The time of the rescue train coupling the fault train;

 $T_{p}$ : The time of fault train being pushed to the specific storage;

 $T_f$ : The time of all the passengers on rescue train and fault train alighting;

 $T_c$ ,  $T_h$ ,  $T_f$  are determined by the operator's proficiency, in this paper we assume the value of these variables is constant. In order to facilitate the establishment of the model, we assume the starting process of the train runs at a uniform acceleration speed, the running process runs at a constant speed, the stopping process runs at a uniform deceleration speed.

$$T_{a} = \begin{cases} \sqrt{2S_{a}(a_{u}+a_{d})/a_{u}a_{d}} & S_{a} \leq V_{r}^{2}(a_{u}+a_{d})/2a_{u}a_{d} \\ (S_{a}/V_{r})+V_{r}(a_{u}+a_{d})/2a_{u}a_{d} & S_{a} > V_{r}^{2}(a_{u}+a_{d})/2a_{u}a_{d} \end{cases}$$
(2)

 $T_p$  is determined by the distance which is from the position where fault train stops to the temporary storage station, the pushing speed is regulated from 25km/h to 35km/h [8], and in this paper, we assume the speed is 30km/h. The pushing process is made of two parts: rescue train pushes fault train to the station where passengers on train get off; and the fault train is pushed to the temporary storage. As is mentioned above, in the first part, we suppose the distance is  $S_c$  and the spent time is  $t_c$ . And in the second part, we suppose the distance is  $S_s$  and the spent time is calculated as follows:

$$t_{c} = \begin{cases} \sqrt{2S_{c}(a_{u}+a_{d})/a_{u}a_{d}} & S_{c} \leq V_{h}^{2}(a_{u}+a_{d})/2a_{u}a_{d} \\ (S_{c}/V_{h})+V_{h}(a_{u}+a_{d})/2a_{u}a_{d} & S_{c} > V_{h}^{2}(a_{u}+a_{d})/2a_{u}a_{d} \end{cases}$$
(3)

$$t_{s} = \begin{cases} \sqrt{2S_{s}(a_{u}+a_{d})/a_{u}a_{d}} & S_{s} \leq V_{h}^{2}(a_{u}+a_{d})/2a_{u}a_{d} \\ (S_{s}/V_{h}) + V_{h}(a_{u}+a_{d})/2a_{u}a_{d} & S_{s} > V_{h}^{2}(a_{u}+a_{d})/2a_{u}a_{d} \end{cases}$$
(4)

Therefore, the total delay time T can be obtained.

## **3.** Train Operation Adjustment Strategy

## **3.1.** Adjustment Strategy after Removing Fault

The traditional adjustment method for delay is adjust the running time in sections, headways between trains and dwell time at stations. The equations below describe the running time in sections, constraints of headway and stopping time of the trains.

$$R_{i,j} = \begin{cases} ar_{j+1}^{i} - de_{j}^{i} & de_{j}^{i} < ar_{j+1}^{i} - R_{\min j} \\ R_{\min j} & de_{j}^{i} < ar_{j+1}^{i} - R_{\min j} \end{cases}$$
(5)

The influence of passenger flow is taken into count. The literature describes the dwelling time has a linear relationship with the number of the passengers at stations.  $t_{minj}$  is the minimum stopping time at station j,  $a_j$  is the extension rate of stopping time caused by delay. Therefore, the dwelling time is:

. .

$$t_{j} = \begin{cases} t_{\max j} & t_{\min j} + a_{j}(d_{i,j} - d_{i-1,j} - D_{i,j} - D_{i-1,j}) > t_{\max j} \\ t_{\min j} + a_{j}(d_{i,j} - d_{i-1,j} - D_{i,j} - D_{i-1,j}) & \text{the other} \end{cases}$$
(6)

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The evacuation of passengers is also added to measures, and the objective function is established and optimized. Optimization objects considered in this paper contains delay time and stranded passengers:

$$\min \mathbf{J} = a_1 \sum_{i=1}^n \sum_{j=1}^m \left( |d\mathbf{e}_j^i - \mathbf{D}\mathbf{e}_j^i| + |a\mathbf{r}_j^i - \mathbf{A}\mathbf{r}_j^i| \right) + a_2 \sum_{i=1}^n \sum_{j=1}^m \mathbf{Fo}_j^i$$
(7)

according to different demands of managers, the proportions a1 and a2 can be adjusted.

The constraints are as follows:

$$de_{j}^{i}-ar_{j}^{i}\geq t_{\min j}$$

$$\tag{8}$$

$$ar_{j+1}^{i}-de_{j}^{i} \ge R_{\min j}$$
(9)

$$ar_{j}^{i+1}-ar_{j}^{i}\geq T_{hwmin}$$
<sup>(10)</sup>

$$de_{i}^{i+1}-de_{i}^{i} \ge T_{hwmin}$$

$$\tag{11}$$

### **3.2.** Short-turning Adjustment Strategy

In this paper, the trains are unable to pass the stations which is behind the fault train. If the trains can not pass following stations after a period of disposing, the trains in the opposite direction can be organized to turn back at certain station to make up the longer interval [8-10]. It is important to determine the turning-back station, the train of turning back and the number of turning-back trains. In order to minimize the effect

of stranded passengers, turning-back station should be close to the point of the fault [11-12]. However, passengers on the turning-back train have to alight at turning-back station, resulting in a sudden increasing passengers at the turning-back station, it will lead to the following trains delay [13]. In this paper, we consider the delay in the opposite direction caused by the turning-back train and the number of stranded passengers as the adjustment target, and optimize short-turning regulation strategy.

## **3.3.** Optimization Algorithm

This paper adopts particle swarm optimization algorithm of linear decreasing to optimize objects. Following Eberhart and Kennedy's naming conventions, D is the dimension of the search space. The  $i^{th}$  particle is represented by  $X_i = (x_{i1}, x_{i2}, \dots, x_{iD})$  and its previous best is  $P_i = (p_{i1}, p_{i2}, \dots, p_{iD})$ . The index of the best in the whole group is g. Each particle in PSO flies in the search space with a velocity which is dynamically adjusted according to its own flying experience and its companions' flying experience [14-16]. w is redesigned according to the reference [17-19]

$$v_i^{k+1} = wv_i^k + c_1 r_1(p_i^k - x_i^k) + c_2 r_2(p_i^k - x_i^k)$$
(12)

$$x_i^{k+1} = x_i^k + v_i^{k+1}$$
(13)

$$w = w_{\max} - \frac{(w_{\max} - w_{\min})}{t_{\max}} * t$$
(14)

Where  $c_1$  and  $c_2$  are two positive constants,  $r_1$  and  $r_2$  are two random functions in the range [0, 1],  $w_{min}$  and  $w_{max}$  are the maximum and minimum value according to expert system,  $t_{max}$  is the maximum iteration, t is the current iteration.

## 4. Simulation and Solution

In this paper, the operating parameters of an urban rail transit are as follows in table 2. The third train has a fault and stops between station 6 and station 7, the fourth train receives the rescue mission, the subway line data is shown in Fig.4. 1<sup>th</sup> station, 3<sup>th</sup> station, 5<sup>th</sup> station, 6th station, 8th station and 10th station are turning-back stations, and the turning-back time is 120s.



Fig.4: Subway line in the case of train fault

Table 2: Parameters in simulation

$S_t$		12		$T_r$				15				
$T_{hw}^0(\mathbf{s})$		240		$T_{hw\min}(\mathbf{s})$				90				
$S_a(\mathbf{m})$		1300		$S_c(\mathbf{m})$				400				
$S_{s}(\mathbf{m})$		2200		$F_m$				1800				
$a_u (\mathrm{m/s^2})$		0.8		$a_d (\mathrm{m/s^2})$				-0.6				
$V_r$ (m/s)		40		$V_h$ (m/s)				30				
Fault train		3 <sup>th</sup>		Rescue train				4 <sup>th</sup>				
S <sub>t</sub>	1	2	3	4	5	6	7	8	9	10	11	12
$t_{\min j}$ (s)	30	25	25	25	30	25	25	25	25	25	25	30
$t_{\max j}(\mathbf{s})$	40	35	35	35	40	35	35	35	35	35	35	40
$V f_j(\mathbf{s})$	1.18	1.31	1.29	1.34	1.37	1.31	1.40	1.27	1.32	1.34	1.29	0
Section	1	2	3	4	5	6	7	8	9	10	11	-
$R_{i,j}^0$ (s)	172	116	226	106	114	161	114	118	241	163	115	-
$R_{\min j}(s)$	166	110	220	100	106	155	109	110	235	155	110	-

## **4.1.** Simulation after Removing Fault

The improved PSO algorithm takes the minimum delays and stranded passengers as the optimization objects. Here we set  $a_1 = 0.4$ ,  $a_2 = 0.6$ , the population of the swarm is 100, the number of iteration is 100. Fig.5 shows the simulation results.



Fig.5: The operation after service restored

In Fig.5, the blue lines and black lines represent scheduled timetable of up trains and down trains, Because of disposing fault, the following trains are backlogged at the stations, and this leads many trains delay and passengers stranded. The following stations can't pass trains during disposing fault and passengers at fault train and rescue train get off at station 6 and 7, that also causes large numbers of passengers stranded at following stations, as shown in Fig.6. After disposing the fault, trains pass the following stations densely. Stranded passengers at stations after each train passing the station are shown in Fig.7.



Fig.6: Stranded passengers when line reopened



Fig.7: Stranded passengers after each train passing station

## 4.2. Simulation Using Short-turning Adjustment Strategy

In this paper, when down trains can't pass the fault position more than five minutes, the up train is assigned to turn back at certain turning-back station. When the line is opened to traffic again, it is regarded as the end time of turning-back operation. According to the operation and line parameters, the location of fault and the time of dealing with emergencies, the turning-back cases can be determined. Case 1: up 5<sup>th</sup> train turns back at 6<sup>th</sup> station. Case 2: up 5<sup>th</sup> and 6<sup>th</sup> trains turn back at 6<sup>th</sup> station. Case 3: up 5<sup>th</sup> train turns back at 5<sup>th</sup> station. Case 4: up 5<sup>th</sup> and 6<sup>th</sup> trains turn back at 5<sup>th</sup> station. Case 5: up 6<sup>th</sup> train turns back at 3<sup>th</sup> station, and case 6: up 6<sup>th</sup> and 7<sup>th</sup> trains turn back at  $3^{th}$  station. The percentage of the delay time and the stranded

passengers which accounts for the total delay time and the total stranded passengers is shown in Fig.8. Based on the optimization objects, the optimal strategy is case 1. Fig.9 shows the operation under the best short-turning strategy. Stranded passengers at stations after each train passing the station are shown in Fig.10.



Fig.9: Operation with optimal short-turning strategy



In Fig.9, the up 5<sup>th</sup> train turns back at station 6, the purple line represents the turn-back of up train., this regulation greatly reduces the number of stranded passengers at the following stations. Meanwhile, as a part of the clear-off passengers are transported by the turn-back train, the number of stranded passengers at the station 6 significantly reduces. So it is available to choose short-turning to relieve congestion when the lines can't operate normally, and it is effective to turn back at large numbers of stranded passenger stations.

### **4.3.** Two Adjustment Strategies Comparisons

By comparing these two different adjustment strategies, it can be seen that the short-turning adjustment can quickly restore the operation to the planned operation. The operation of the 9<sup>th</sup> train downstream in Fig.9 basically resumes the planned operation, but the operation of the 15<sup>th</sup> train in Fig.5 has not been restored to the planned operation. Turning-back operation of the up train makes up for the problem of excessive running interval at following stations caused by the faulty train, as a part of the clear-off passengers are transported

by the turn-back train, the number of stranded passengers at the station 6 significantly reduces. Compared with Fig.7, short-turning adjustment strategy can quickly reduce the detention of platform passengers. Simulation results indicate the effectiveness of short-turning strategy when the service of traffic disrupts. So it is available to choose short-turning to relieve congestion when the lines can't operate normally, and it is effective to turn back at large numbers of stranded passenger stations.

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